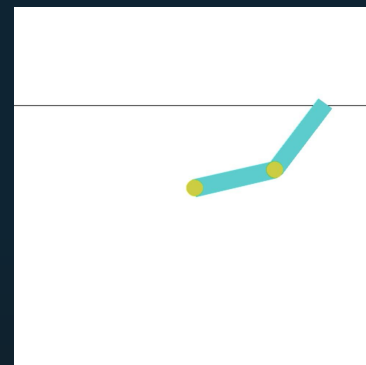
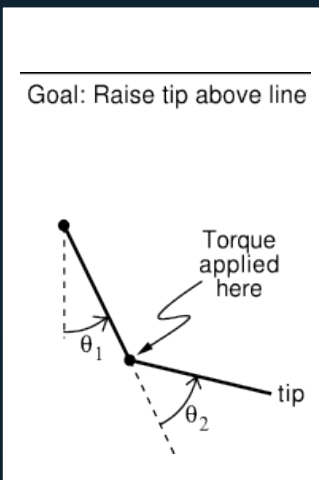
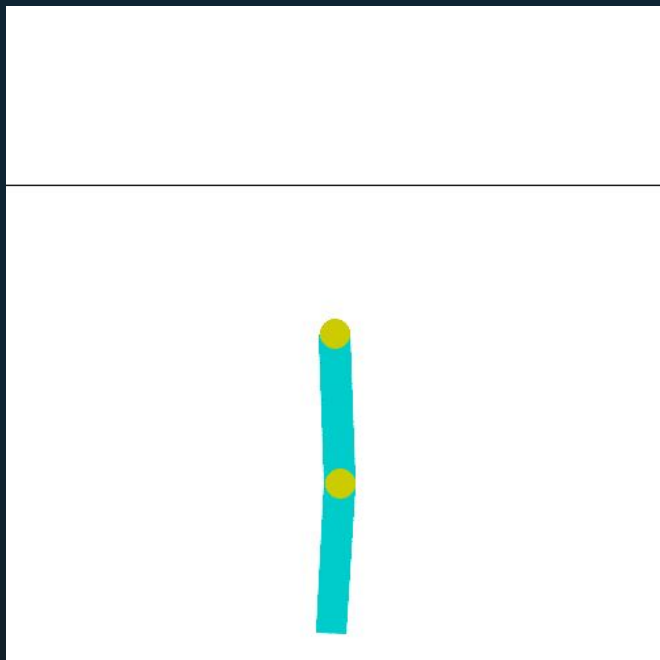


Range-to-Range Regression

Propagating
Uncertainty in
Environment Model

Zoe Shao, L.A.C.E. Lab
Advisor: Erin Talvitie

Reinforcement Learning



Goal: reach the top in fewest frames

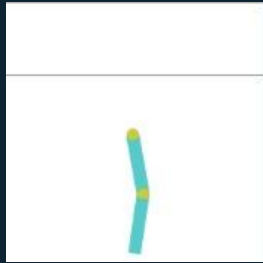
Source: [Gym Documentation - Acrobot](#)

What is Reinforcement Learning (RL)?

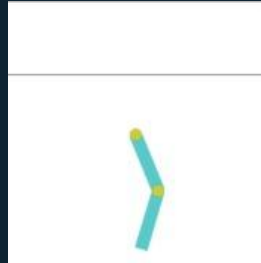


How does the agent learn?

Sample From Real Environment



Torque 1



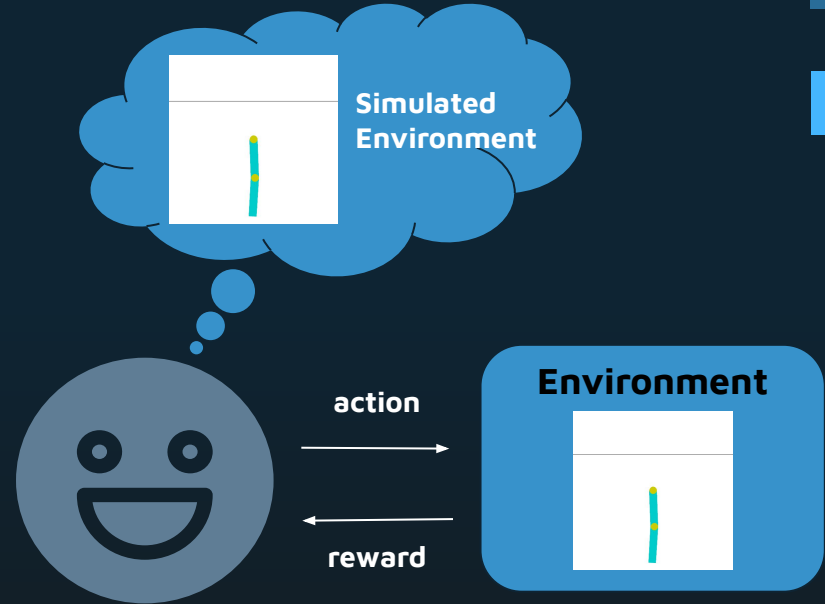
Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

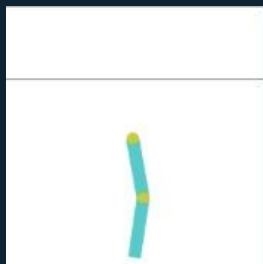
Target: $1+80 = 81$



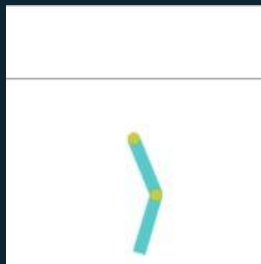
* Est. is the estimate number of frames from the goal

How does the agent learn?

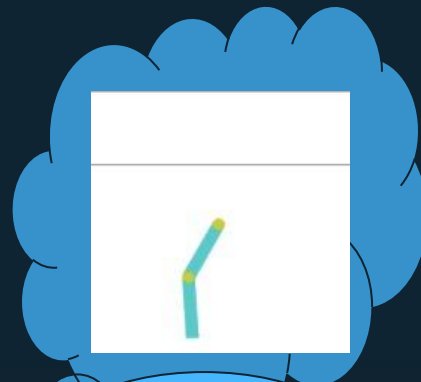
Sample From Real Environment



Torque 1



Torque 1



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

Est.

Torque 1: 85
Torque 0: 60
Torque -1: 95

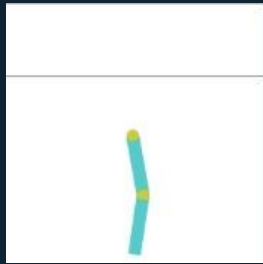
Target: $1+80 = 81$

Target: $2+60 = 62$

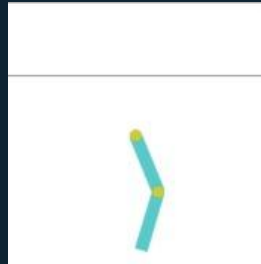
* Est. is the estimate number of frames from the goal

Planning

Sample From Real Environment



Torque 1



Torque 1



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

Est.

Torque 1: 85
Torque 0: 60
Torque -1: 95

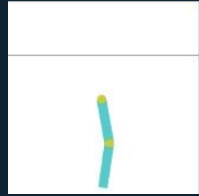
Target: $1+80 = 81$

Target: $2+60 = 62$

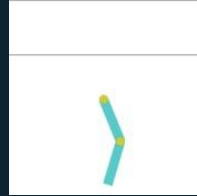
* Est. is the estimate number of frames from the goal

3-Step Planning

Sample From Real Environment



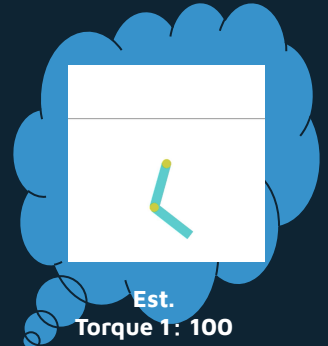
Torque 1



Torque 1



Torque 0



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

Est.

Torque 1: 85
Torque 0: 60
Torque -1: 95

Est.

Torque 1: 100
Torque 0: 45
Torque -1: 60

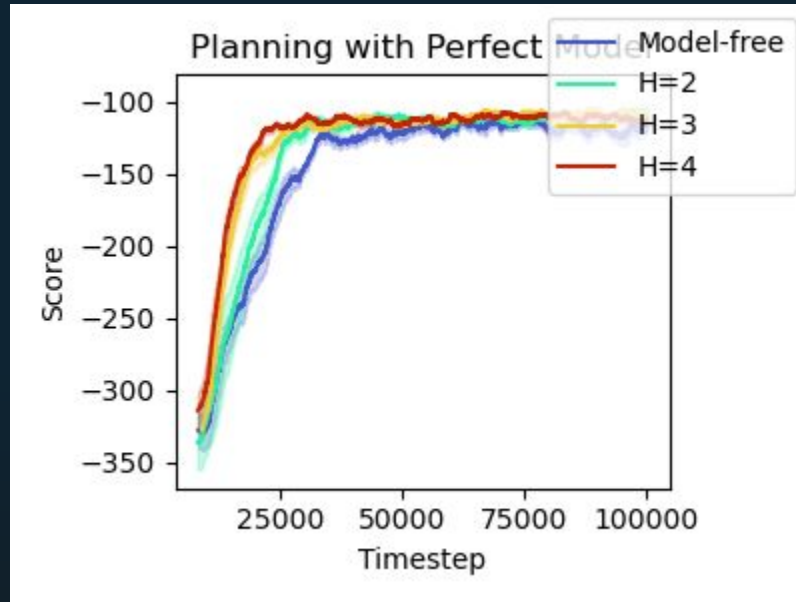
Target: 1+80
= 81

Target: 2+60
= 62

Target: 3+48
= 48

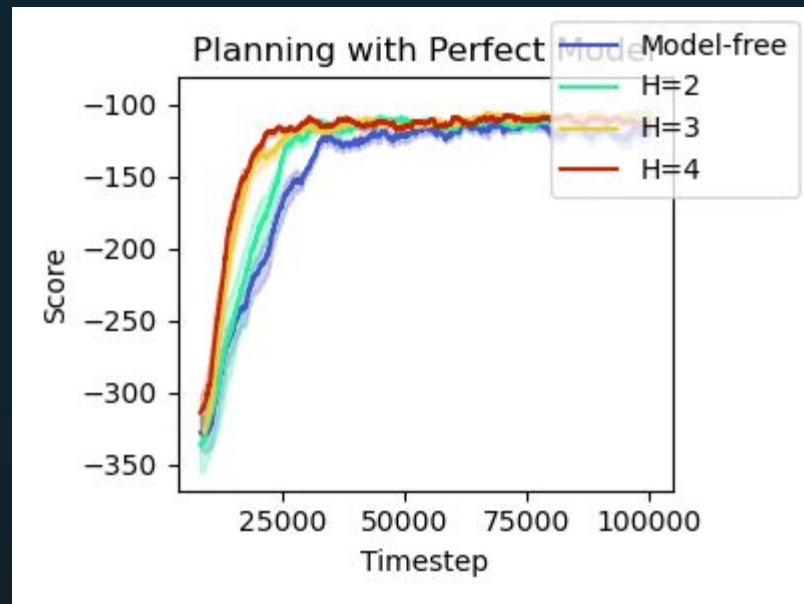
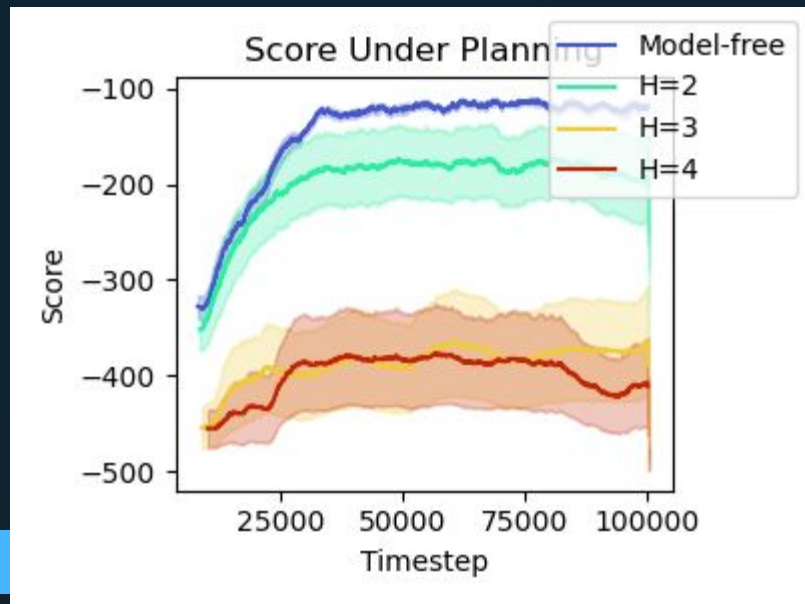
* Est. is the estimate number of frames from the goal

Planning Helps



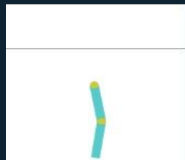
Planning with Perfect Model

Planning Not Helping?

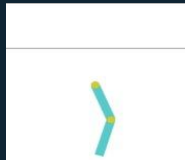


Planning Not Helping?

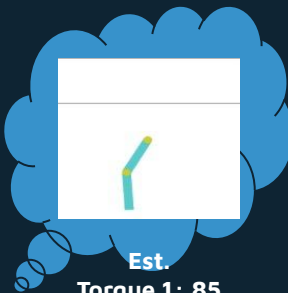
Sample From Real Environment



Torque 1 →



Torque 1 →



Torque 0 →



Est.

Torque 1: 90

Torque 0: 60

Torque -1: 90

Est.

Torque 1: 80

Torque 0: 90

Torque -1: 100

Est.

Torque 1: 85

Torque 0: 60

Torque -1: 95

Est.

Torque 1: 100

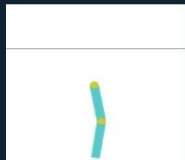
Torque 0: 45

Torque -1: 60

* Est. is the estimate number of frames from the goal

Planning Not Helping?

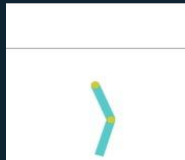
Sample From Real Environment



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

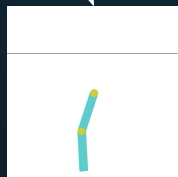
Torque 1



Est.

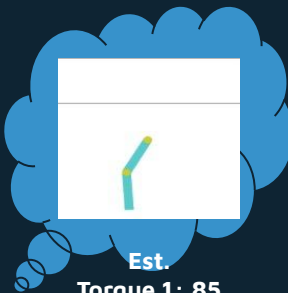
Torque 1: 80
Torque 0: 90
Torque -1: 100

Torque 1



Est.

Torque 1: 80
Torque 0: 70
Torque -1: 90



Est.

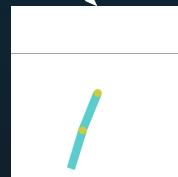
Torque 1: 85
Torque 0: 60
Torque -1: 95

Torque 0



Est.

Torque 1: 100
Torque 0: 45
Torque -1: 60



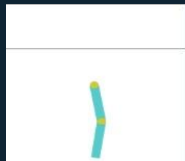
Est.

Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

Planning Not Helping?

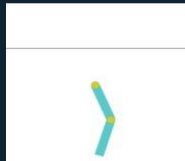
Sample From Real Environment



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

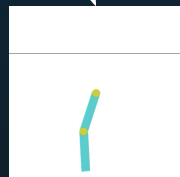
Torque 1



Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

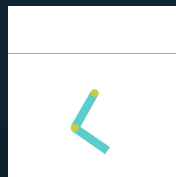
Torque 1



Est.

Torque 1: 80
Torque 0: 70
Torque -1: 90

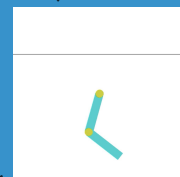
Torque 0



Est.

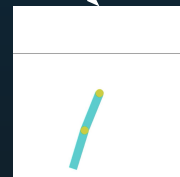
Torque 1: 70
Torque 0: 60
Torque -1: 80

Torque 0



Est.

Torque 1: 100
Torque 0: 45
Torque -1: 60



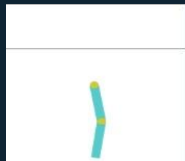
Est.

Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

Selective Planning

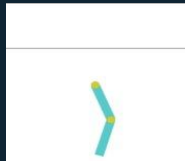
Sample From Real Environment



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

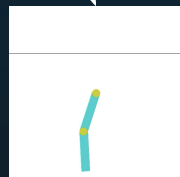
Torque 1



Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

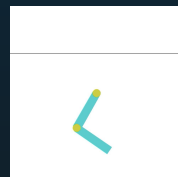
Torque 1



Est.

Torque 1: 80
Torque 0: 70
Torque -1: 90

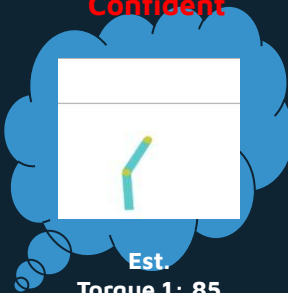
Torque 0



Est.

Torque 1: 70
Torque 0: 60
Torque -1: 80

Confident



Est.

Torque 1: 85
Torque 0: 60
Torque -1: 95

Torque 0



Not Confident

Est.

Torque 1: 100
Torque 0: 45
Torque -1: 60



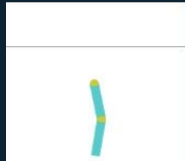
Est.

Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

Selective Planning

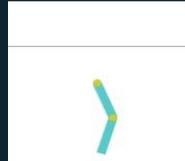
Sample From Real Environment



Est.

Torque 1: 90
Torque 0: 60
Torque -1: 90

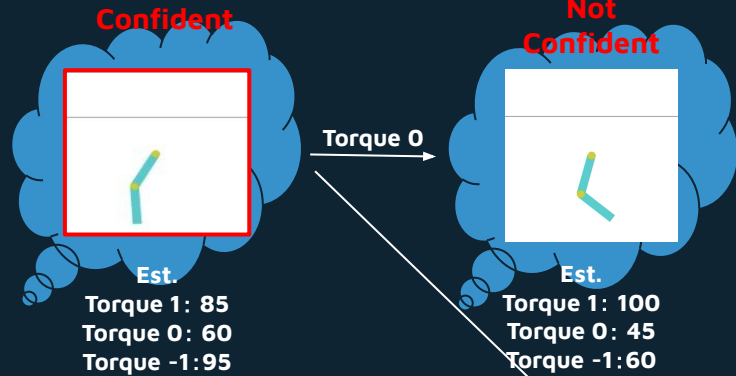
Torque 1



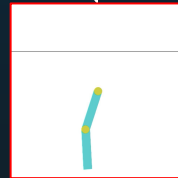
Est.

Torque 1: 80
Torque 0: 90
Torque -1: 100

Torque 1



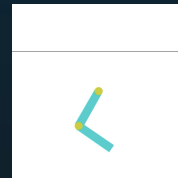
How to measure the uncertainty?



Est.

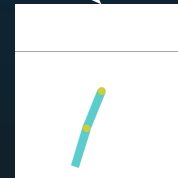
Torque 1: 80
Torque 0: 70
Torque -1: 90

Torque 0



Est.

Torque 1: 70
Torque 0: 60
Torque -1: 80



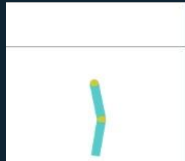
Est.

Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

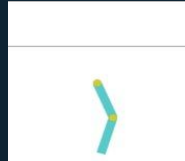
Selective Planning

Sample From Real Environment



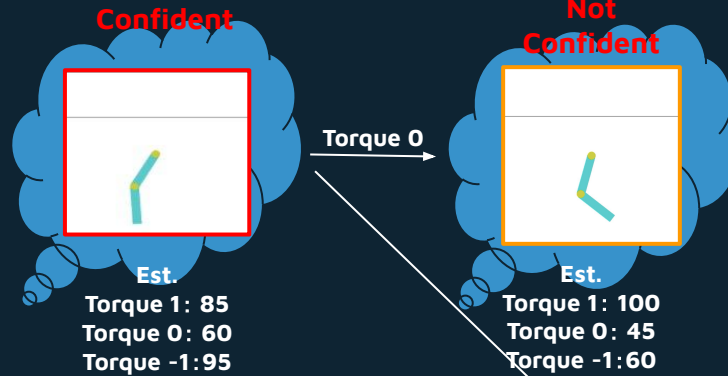
Est.
Torque 1: 90
Torque 0: 60
Torque -1: 90

Torque 1



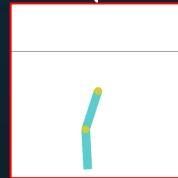
Est.
Torque 1: 80
Torque 0: 90
Torque -1: 100

Torque 1



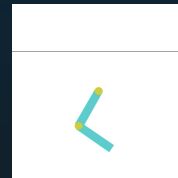
How to measure the uncertainty?

→ One-Step State Error

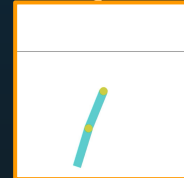


Est.
Torque 1: 80
Torque 0: 70
Torque -1: 90

Torque 0



Est.
Torque 1: 70
Torque 0: 60
Torque -1: 80

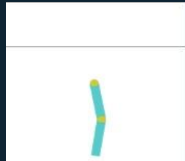


Est.
Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

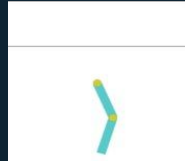
Selective Planning

Sample From Real Environment



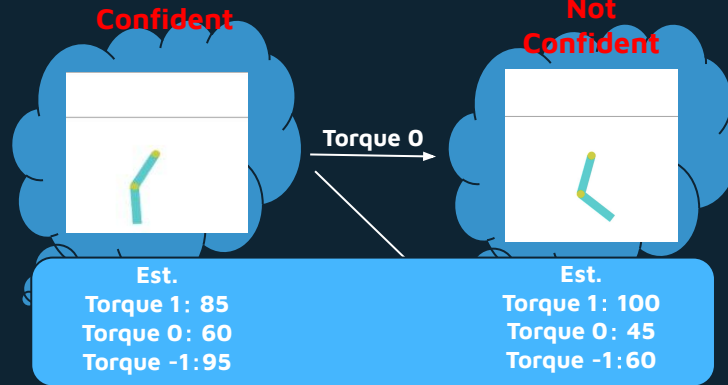
Est.
Torque 1: 90
Torque 0: 60
Torque -1: 90

Torque 1



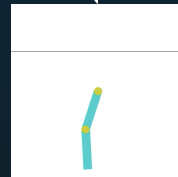
Est.
Torque 1: 80
Torque 0: 90
Torque -1: 100

Torque 1



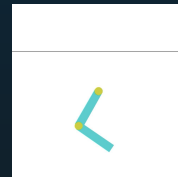
How to measure the uncertainty?

- One-Step State Error
- Target Error

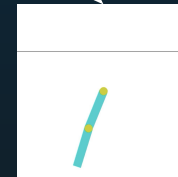


Est.
Torque 1: 80
Torque 0: 70
Torque -1: 90

Torque 0



Est.
Torque 1: 70
Torque 0: 60
Torque -1: 80

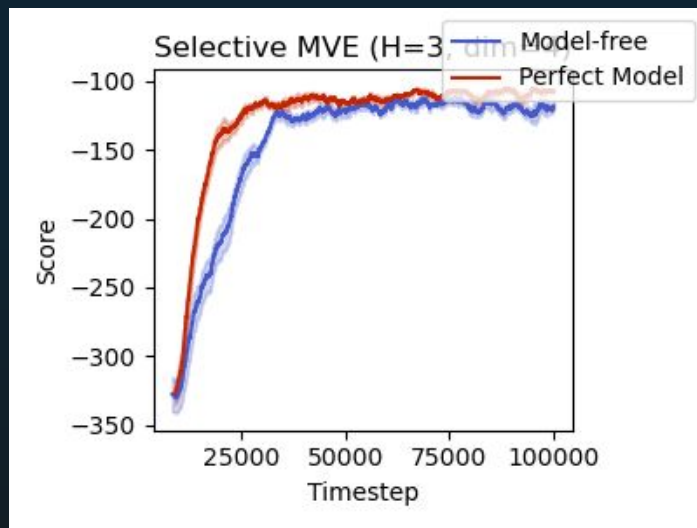


Est.
Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

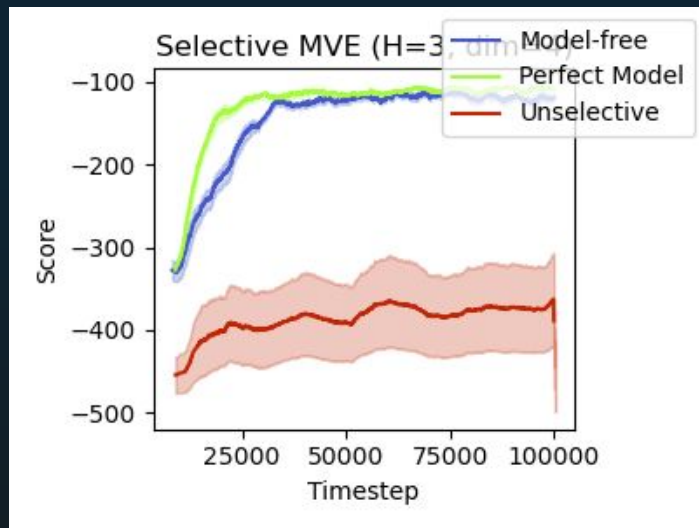
Testing Hypothesis

- State and target can be used as uncertainty signal to measure how confident model is
- Oracle experiment
 - ◆ Assume differences are known and weigh experiences differently accordingly
 - ◆ For one-step state error, we accumulate them through planning



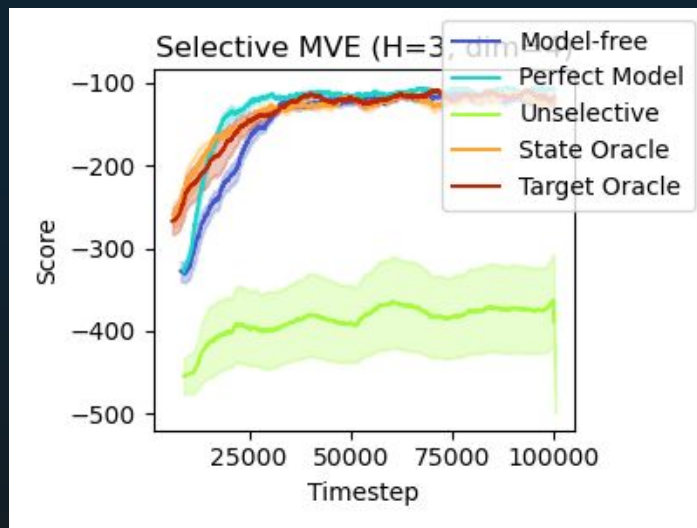
Testing Hypothesis

- State and target can be used as uncertainty signal to measure how confident model is
- Oracle experiment
 - ◆ Assume differences are known and weigh experiences differently accordingly
 - ◆ For one-step state error, we accumulate them through planning



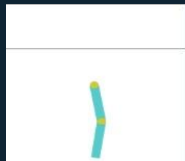
Testing Hypothesis

- State and target can be used as uncertainty signal to measure how confident model is
- Oracle experiment
 - ◆ Assume differences are known and weigh experiences differently accordingly
 - ◆ For one-step state error, we accumulate them through planning



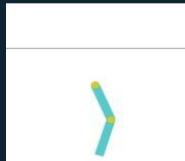
New Idea: Planning With Range

Sample From Real Environment



Est.
Torque 1: 90
Torque 0: 60
Torque -1: 90

Torque 1



Est.
Torque 1: 80
Torque 0: 90
Torque -1: 100

Torque 1

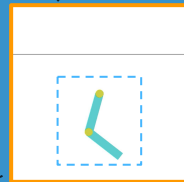
Confident



Est.
Torque 1: 85
Torque 0: 60
Torque -1: 95

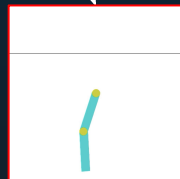
Torque 0

Not Confident



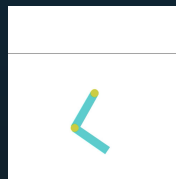
Est.
Torque 1: 100
Torque 0: 45
Torque -1: 60

Use range to let the model take uncertainty from last frame into account

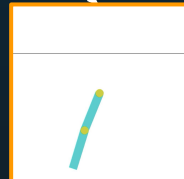


Est.
Torque 1: 80
Torque 0: 70
Torque -1: 90

Torque 0



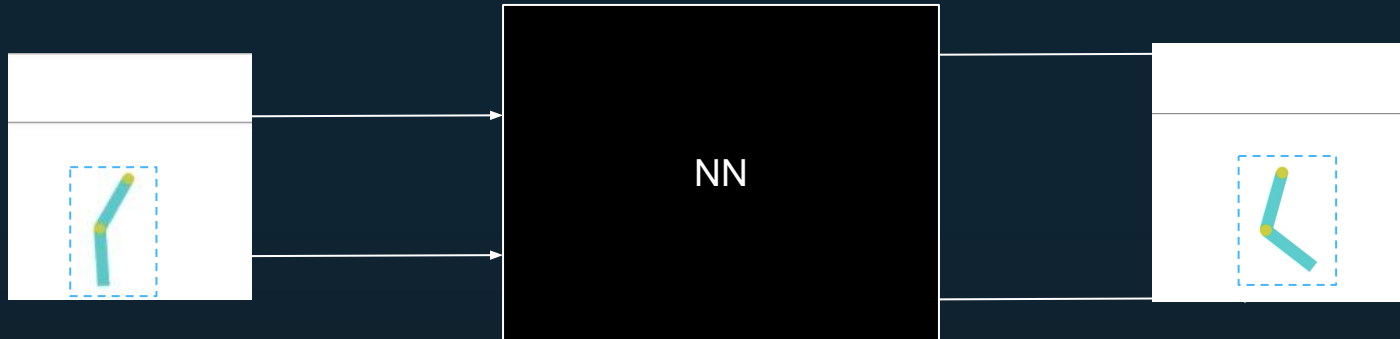
Est.
Torque 1: 70
Torque 0: 60
Torque -1: 80



Est.
Torque 1: 90
Torque 0: 70
Torque -1: 80

* Est. is the estimate number of frames from the goal

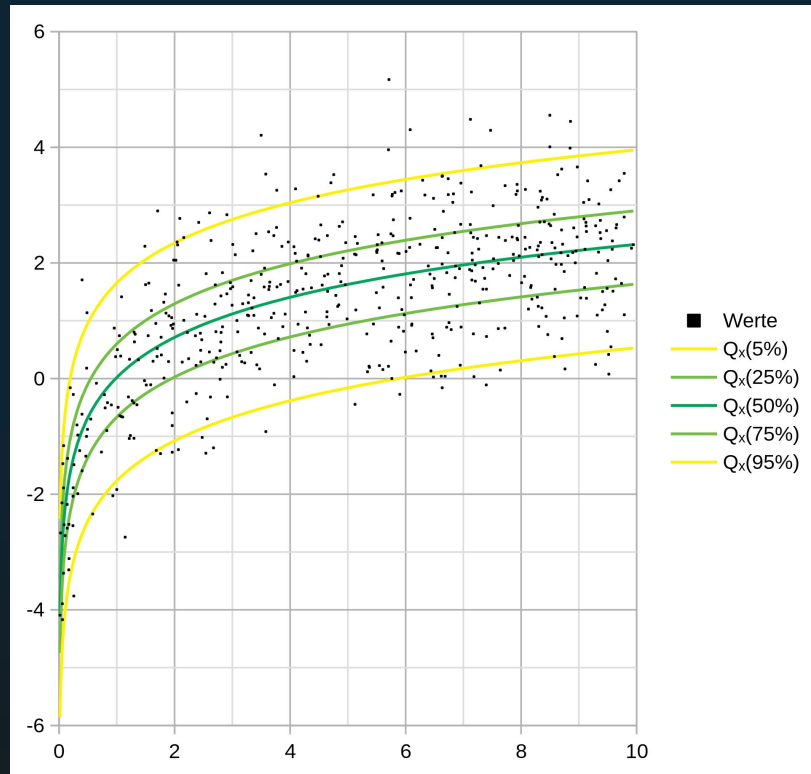
Approach: Neural Networks with Quantile Regression



Approach: Neural Networks with Quantile Regression



Source: [Ready to Score 1500+ on S.A.T? - Boost Your S.A.T Score Quickly](#)

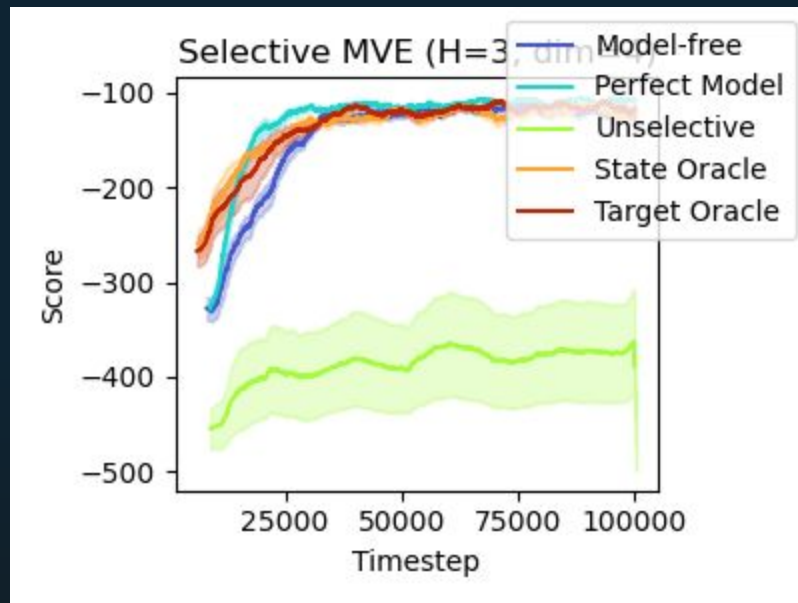


Source: https://en.wikipedia.org/wiki/Quantile_regression#Intuition

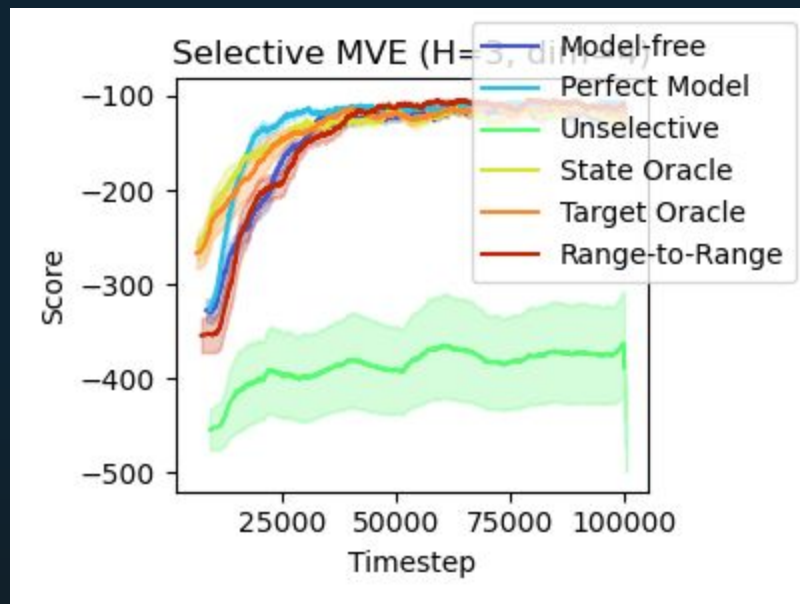
Approach: Neural Networks with Quantile Regression



Preliminary Results



Preliminary Results



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